

# Negative Thermal Expansion HfV<sub>2</sub>O<sub>7</sub> Nanostructures for Alleviation of Thermal Stress in Nanocomposite Coatings

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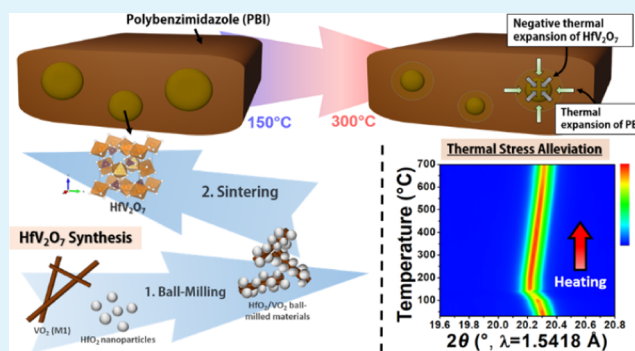
Supporting Information

**ABSTRACT:** A primary mode of failure of thin-film coatings is the mismatch in thermal expansion coefficients of the substrate and the coating, which results in accumulation of interfacial stresses and ultimately in film delamination. While much attention has been devoted to modulation of interfacial bonding to mitigate delamination, current strategies are constrained in their generalizability and have had limited success in imbuing resistance to prolonged thermal cycling. We demonstrate here the incorporation of rigid thermal expansion compensators within polymeric films as a generalizable strategy for minimizing thermal mismatch with the substrate. Nanostructures of the isotropic negative thermal expansion (NTE) material HfV<sub>2</sub>O<sub>7</sub> have been prepared based on the reaction of nanoparticulate precursors. The NTE behavior, derived from transverse oxygen displacement within the cubic structure, has been examined using temperature-variant powder X-ray diffraction, Raman spectroscopy, electron microscopy, and selected-area electron diffraction measurements. HfV<sub>2</sub>O<sub>7</sub> initially crystallizes in a 3 × 3 × 3 superlattice but undergoes phase transformations to stabilize a cubic structure that exhibits strong and isotropic NTE with a coefficient of thermal expansion (CTE) =  $-6.7 \times 10^{-6} \text{ } ^\circ\text{C}^{-1}$  across an extended temperature range of 130–700 °C. Incorporation of HfV<sub>2</sub>O<sub>7</sub> in a high-temperature thermoset polybenzimidazole enables the reduction of compressive stress by 67.3% for a relatively small loading of 26.6 vol % HfV<sub>2</sub>O<sub>7</sub>. Based on a composite model, we demonstrate that HfV<sub>2</sub>O<sub>7</sub> can reduce the thermal expansion coefficient of polymer nanocomposite films, even at low volume fractions, as a result of its substantially higher elastic modulus compared to the continuous polymer matrix. By changing the volume fraction of HfV<sub>2</sub>O<sub>7</sub>, the overall coefficients of thermal expansion of the film can be tuned to match a range of substrates, thereby mitigating thermal stresses and resolving a fundamental challenge for high-temperature composites and nanocomposite coatings.

**KEYWORDS:** hafnium pyrovanadate, nanostructure, negative thermal expansion, *in situ* TEM, thermal stress

## INTRODUCTION

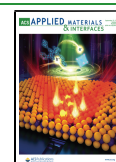
Most materials expand in volume in response to thermal excitation; the specific directionality and magnitude of expansion of a solid derives from a complex interplay of phonon dispersion, lattice structure, and electronic structure.<sup>1,2</sup> The Grüneisen parameter, a dimensionless number, clumps together different thermodynamic quantities in a singular metric that provides a population-averaged view of thermally triggered nonlinearities in phonon dynamics.<sup>3,4</sup> From a practical perspective, thermal expansion is strongly implicated in materials degradation because of stresses arising from thermal gradients. Such stresses are compounded during periods of prolonged operation, giving rise to fatigue and failure.<sup>5,6</sup> In laminar composites and coatings, differentials in the coefficient of thermal expansion (CTE) of different materials give rise to interfacial strain and debonding upon thermal cycling.<sup>7</sup> As such, considerable effort has focused on the design and discovery of negative thermal expansion (NTE)



materials, which are characterized by volume contraction upon heating, and thus upon incorporation within blended composites, provide a means of buffering undesirable thermal expansion.<sup>1,2,8–10</sup> In this work, we describe the facile synthesis of an NTE material, HfV<sub>2</sub>O<sub>7</sub>, from nanoparticle precursors; illustrate the NTE properties across a 570 °C temperature range using variable-temperature X-ray diffraction (XRD), Raman spectroscopy, and high-resolution transmission electron microscopy (HRTEM); and demonstrate the sharply reduced stress accumulation in polymer nanocomposite

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coatings embedding HfV<sub>2</sub>O<sub>7</sub> upon thermal cycling using multibeam optical sensor measurements.

For a specific NTE material to be of value in thermal expansion compensation, the following characteristics need to be considered: (i) the magnitude of the NTE coefficient; (ii) the directionality (isotropic or anisotropic) of NTE; and (iii) the temperature range over which NTE is manifested. The most commonly studied materials such as Sc<sub>2</sub>(WO<sub>4</sub>)<sub>3</sub> exhibit anisotropic NTE over a relatively narrow range of temperatures,<sup>11–15</sup> which limits their practical utility in thermal expansion compensators.<sup>11,16,17</sup> MV<sub>2</sub>O<sub>7</sub> (M = Zr, Hf) compounds show quasi-isotropic NTE as a result of their cubic crystal structure. These compounds further exhibit NTE behavior across a broad temperature range and are wide-band-gap materials that have attracted considerable interest as thermally responsive components in the design of zero-thermal-expansion composites.

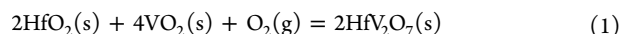
MV<sub>2</sub>O<sub>7</sub> crystallized in the  $P\bar{a}3$  space group comprises interconnected corner-sharing MO<sub>6</sub> octahedra and VO<sub>4</sub> tetrahedra; adjacent VO<sub>4</sub> tetrahedra are linked by corner sharing to form a V<sub>2</sub>O<sub>7</sub> unit connected by a bridging oxygen (O<sub>3</sub>V–O–VO<sub>3</sub>).<sup>11,17–19</sup> MV<sub>2</sub>O<sub>7</sub> compounds adopt a 3 × 3 × 3 superstructure at room temperature and transform to a 1 × 1 × 1 cubic structure above about 100 °C, foreshadowing the manifestation of NTE behavior. In the low-temperature superstructure, four of the six crystallographically unique V<sub>2</sub>O<sub>7</sub> groups are distorted away from 180°, whereas in the cubic structure, all of the V–O–V bridging angles are 180°.<sup>19,20</sup> This increasing of symmetry activates dynamic transverse vibrations of bridging oxygen atoms; these phonon modes have been directly implicated in underpinning a pronounced lattice contraction.<sup>11</sup> ZrV<sub>2</sub>O<sub>7</sub> has a CTE of ca.  $-7.0 \times 10^{-6} \text{ }^\circ\text{C}^{-1}$  in the range of 100–600 °C; however, an abnormal increase in NTE is observed above 600 °C as a result of a phase transition.<sup>19</sup> The thermal expansion of ZrV<sub>2</sub>O<sub>7</sub> has been extensively tailored by substitution methods, such as single-site substitutions replacing V by P, Mo, and W,<sup>21–24</sup> or Zr by Hf and (Nb, Y),<sup>18,25</sup> as well as dual-site substitutions where Zr/V have been replaced by Fe/Mo, Fe/P, Cu/P, etc.<sup>4,26,27</sup> Substitution methods enable modulation of the temperature range of the NTE. For example, a phase-transition temperature as low as  $-48 \text{ }^\circ\text{C}$  is accessible with Mo substitution of ZrV<sub>2</sub>O<sub>7</sub>.<sup>21</sup> However, substitution can sometimes result in the diminution of the NTE coefficient and shrink the NTE window.<sup>21,22,24</sup> Furthermore, the intrinsic cubic symmetry of MV<sub>2</sub>O<sub>7</sub> is broken as a result of some substitutions, such as in the case of W-substituted and Cu/P-substituted MV<sub>2</sub>O<sub>7</sub>.<sup>4,22</sup> HfV<sub>2</sub>O<sub>7</sub> has been reported to have a somewhat higher CTE of ca.  $-7.2 \times 10^{-6} \text{ }^\circ\text{C}^{-1}$  as compared to ZrV<sub>2</sub>O<sub>7</sub>, but has hitherto been studied only within a limited temperature range.<sup>18</sup> The applicability of this material in nanocomposites remains to be elucidated in the absence of viable synthesis routes to nanostructures that can be incorporated as thermal expansion compensators.<sup>28</sup>

Conventional solid-state synthesis routes to HfV<sub>2</sub>O<sub>7</sub> require high temperatures, yield considerable impurity fractions, and as is typical of ceramic processing methods, yield micron-sized polycrystalline products that are unsuitable for incorporation within nanocomposites or coatings.<sup>18,29–31</sup> In this article, we demonstrate a facile solid-state synthesis route to phase-pure single-crystalline nanoparticles of HfV<sub>2</sub>O<sub>7</sub> from reaction mixtures comprising HfO<sub>2</sub> and VO<sub>2</sub> nanoparticles. The NTE behavior of HfV<sub>2</sub>O<sub>7</sub> has been investigated from 30 to 700 °C

using temperature-dependent XRD (coupled with Rietveld refinements to derive lattice parameters), Raman spectroscopy, transmission electron microscopy, and selected-area electron diffraction (SAED). The synthesized HfV<sub>2</sub>O<sub>7</sub> nanoparticles have been embedded as fillers within thin films of polybenzimidazole (PBI), a high-glass-transition-temperature engineered thermoplastic to demonstrate its application as a thermal expansion compensator. The compressive stress induced by the thermal expansion of PBI is reduced by as much as 67.3% upon thermal cycling in the 150–300 °C temperature range for 26.6 vol % loading of HfV<sub>2</sub>O<sub>7</sub>.

## ■ EXPERIMENTAL SECTION

**HfV<sub>2</sub>O<sub>7</sub> Synthesis.** Hafnium pyrovanadate was prepared in nanocrystalline form based on the solid-state reaction of HfO<sub>2</sub> and VO<sub>2</sub> as per



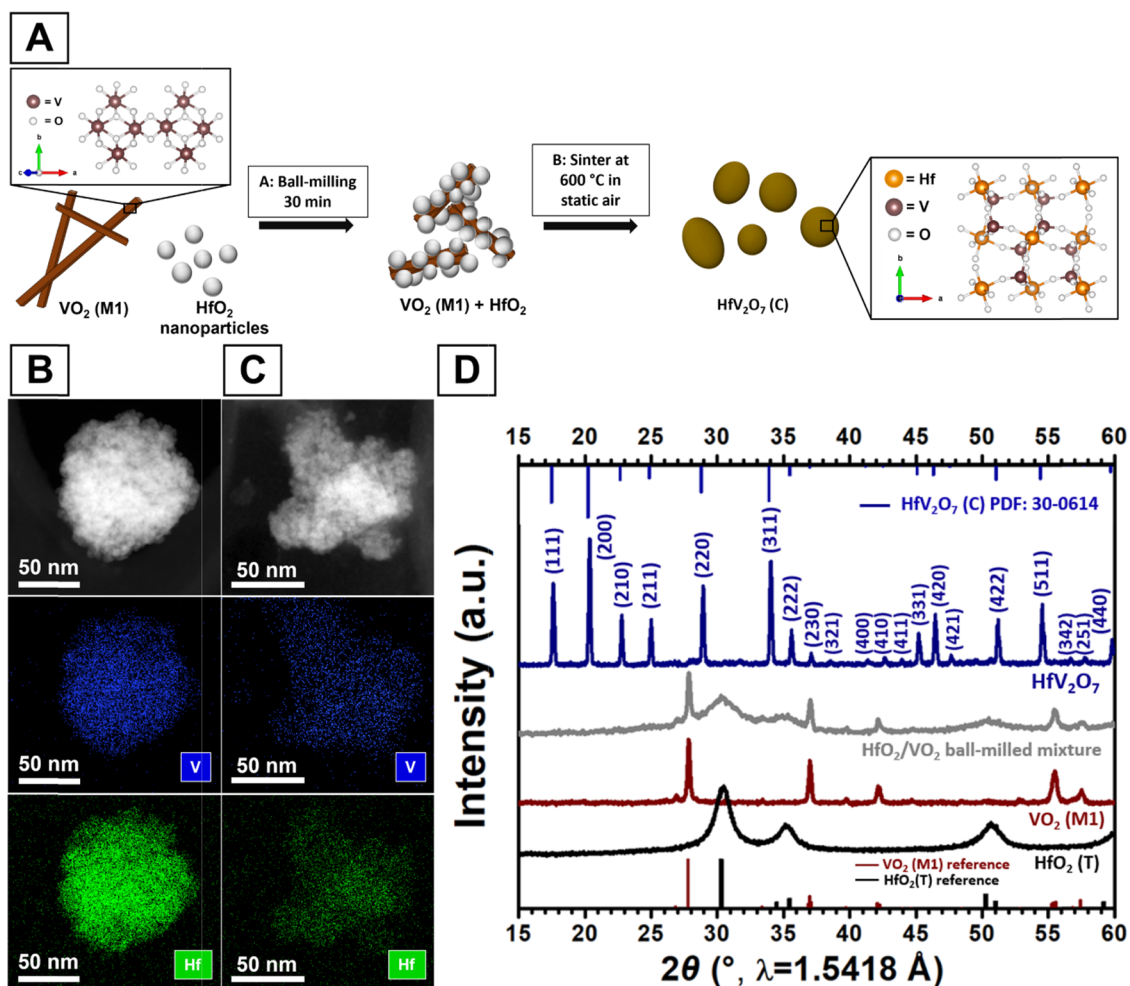
VO<sub>2</sub> crystallized in the M<sub>1</sub> monoclinic phase was purchased from Sigma-Aldrich. HfO<sub>2</sub> nanoparticles were synthesized using hydrothermal methods.<sup>32</sup> In brief, HfCl<sub>4</sub> was dissolved in 3 M NaOH aqueous solution and transferred into a poly(tetrafluoroethylene)-lined autoclave. The sealed autoclave was heated at 120 °C and maintained for 6 or 24 h to produce tetragonal or monoclinic HfO<sub>2</sub>, respectively. The white powder products were retrieved by centrifugation and dried at 60 °C for 4 h. Bulk HfO<sub>2</sub> with crystallite dimensions of 120 ± 26 nm crystallized in the monoclinic phase was purchased from Sigma-Aldrich for comparison.

Stoichiometric mixtures of HfO<sub>2</sub> and VO<sub>2</sub> (total mass = 112.9 mg) were added to a 0.5 × 1 in.<sup>2</sup> polystyrene grinding vial with three 3.0 mm-sized yttria-stabilized zirconia balls and then ball-milled for 30 min at a speed of 1060 cycles/min in an 8000D Mixer/Mill. The HfO<sub>2</sub>/VO<sub>2</sub> ball-milled materials were placed in a porcelain combustion boat and sintered within a tube furnace under a static air ambient at a heating rate of 60 °C/min to 600 °C. The furnace was maintained at 600 °C for 30 min. The light brown products were isolated by cooling under ambient conditions to room temperature.

**PBI-HfV<sub>2</sub>O<sub>7</sub> Nanocomposite Films.** PBI was sourced from PBI Performance Products, Inc. (Charlotte, NC). Nanocomposite formulations were prepared by dispersing 2.3, 4.6, and 9.3 mg of HfV<sub>2</sub>O<sub>7</sub> nanoparticles within 100 μL of 9 wt % PBI/dimethylacetamide (DMAc) solution using a Branson S510R-MT ultrasonicator for 30 min. These masses correspond to 8.4, 15.3, and 26.6 vol % of HfV<sub>2</sub>O<sub>7</sub> in PBI. Control samples were prepared without addition of HfV<sub>2</sub>O<sub>7</sub>.

Prior to coating the HfV<sub>2</sub>O<sub>7</sub>/PBI dispersion in DMAc, a Si wafer substrate with a thickness of 280 μm and a diameter of 50.8 mm was heated and maintained at 150 °C for 10 min on a hot plate. The (100) silicon wafers (resistance of 1–10 Ω/cm) were purchased from University Wafer, Inc. The dispersion was cast onto the substrate at 150 °C using a doctor blade coater. After casting, the film was cured at 150 °C for 10 min.

**Structural Characterization.** Powder X-ray diffraction (XRD) patterns were recorded using a Bruker D8 Advance Eco X-ray powder diffractometer equipped with a Lynxeye detector (25 kV, 40 mA) and a Cu Kα (λ = 1.5418 Å) source. In situ powder X-ray diffraction (XRD) experiments were performed using a Bruker D8-Vario X-ray powder diffractometer equipped with a Cu Kα (λ = 1.5418 Å) source operated at a 40 kV accelerating voltage with a 25 mA current. An MTC oven attachment was used for the heating experiments, which were performed under a flowing N<sub>2</sub> (40 sccm) environment, with patterns recorded at 50 °C intervals. Field emission transmission electron microscopy (FE-TEM) images were recorded on an FEI TECNAI G<sup>2</sup> F20 TEM instrument operated with an accelerating voltage of 200 kV. In situ heating Raman experiments were performed using a Jobin-Yvon HORIBA LabRAM HR800 instrument coupled to an Olympus BX41 microscope and a Linkam THMS600 temperature control stage (heating rate = 2 °C/min). Raman spectra were



**Figure 1.** Direct synthesis of  $\text{HfV}_2\text{O}_7$ . (A) Schematic illustration of synthesis process. Ball-milling  $\text{HfO}_2$  nanoparticles and  $\text{VO}_2$  nanorods (shown in XRD pattern) at a molar ratio of 1:2 ( $\text{HfO}_2/\text{VO}_2$ ) followed by annealing under static air within a tube furnace yields phase-pure  $\text{HfV}_2\text{O}_7$  nanostructures. HAADF-STEM image and EDS elemental mapping images of (B) monoclinic  $\text{HfO}_2/\text{VO}_2$  and (C) tetragonal  $\text{HfO}_2/\text{VO}_2$  ball-milled mixtures. (D) Powder XRD patterns of the precursor  $\text{HfO}_2$  nanoparticles and  $\text{VO}_2$  nanorods, ball-milled mixture, and  $\text{HfV}_2\text{O}_7$  product. The major reflections of  $\text{HfV}_2\text{O}_7$  were indexed as per PDF: 30-0614.

acquired with excitation from the 514.5 nm line of an Ar-ion laser. Endothermic phase transitions were analyzed by differential scanning calorimetry (DSC, Q2000, TA Instruments) from 30 to 150 °C at a scan rate of 5 °C/min using Tzero aluminum pans under a flowing Ar atmosphere.

High-angle annular dark-field imaging (HAADF) in scanning transmission electron microscopy (STEM) mode was performed using an FEI-TALOS F200X microscope. STEM–energy-dispersive spectrometry (EDS) compositional maps and spectra generated from the maps were collected using four in-column SDD Super-X detectors in the TEM.

**In Situ Heating in STEM.** A small amount of the as-synthesized  $\text{HfV}_2\text{O}_7$  powder sample was dispersed in high-purity chloroform (Sigma-Aldrich) and ultrasonicated for 30 min. Then, 10  $\mu\text{L}$  of the diluted solution mixture was drop-cast onto a Protochips heating e-chip taking care to ensure that the sample did not contact multiple gold leads to short-circuit the e-chip. The drop-cast e-chips were annealed at 160 °C for 8 h in vacuum ( $\sim 10^{-5}$  Torr) prior to the STEM characterization to burn off any contaminants on the e-chip. In situ heating TEM experiments were performed using a Nion UltraSTEM 100 (U 100) at 100 kV using the Protochips Fusion heating system.

**Mechanical Characterization.** The curvature of a Si substrate ( $\Delta K$ ) with a  $\text{HfV}_2\text{O}_7$ /PBI film coating was measured during thermal cycling using a multibeam optical stress sensor (MOS) from *k*-Space Associates. A Linkam THMS600 temperature control stage was

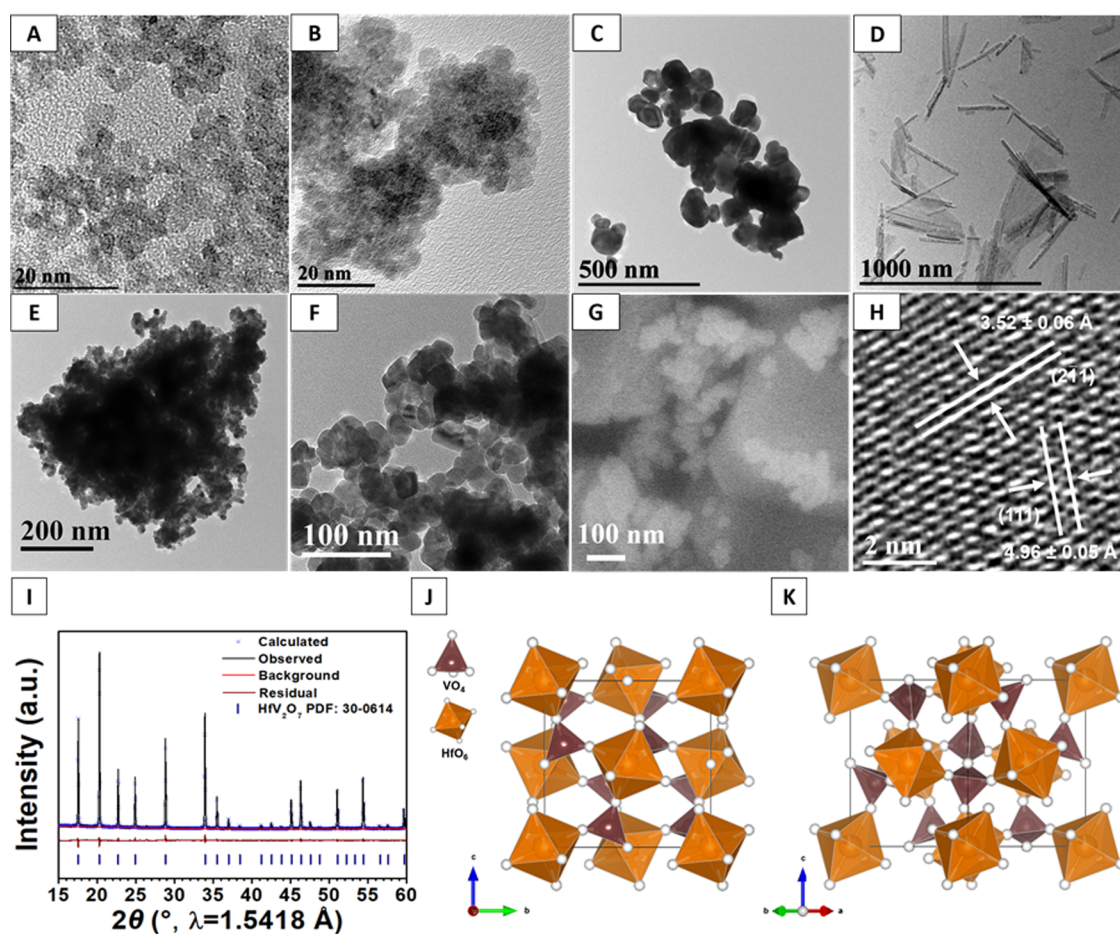
placed on an antivibration table during thermal cycling and curvature measurements. Using Stoney's equation, the average stress change in the thin film upon thermal cycling is<sup>33,34</sup>

$$\Delta\sigma = \frac{E_s h_s^2}{6h_f(1-\nu_s)} \Delta K \quad (2)$$

where  $E_s$  is the elastic modulus of the silicon substrate ( $E_s = 195$  GPa),  $h_s$  is the thickness of the substrate ( $h_s = 0.28$  mm),  $\nu_s$  is the Poisson's ratio of the substrate ( $\nu_s = 0.2$ ), and  $h_f$  is the thickness of thin-film electrode (measured via profilometry). The thicknesses of the  $\text{HfV}_2\text{O}_7$ /PBI films used in the experiments are 7.55  $\mu\text{m}$  (0 vol %  $\text{HfV}_2\text{O}_7$ ), 7.68  $\mu\text{m}$  (8.4 vol %  $\text{HfV}_2\text{O}_7$ ), 6.25  $\mu\text{m}$  (15.3 vol %  $\text{HfV}_2\text{O}_7$ ), and 8.69  $\mu\text{m}$  (26.6 vol %  $\text{HfV}_2\text{O}_7$ ). In this study, we take  $h_f$  as constant during each experiment such that the stress calculated is the nominal (engineering) in-plane stress. Throughout this study, the sign convention is negative for compressive stress and positive for tensile stress.

## RESULTS AND DISCUSSION

Figure 1A illustrates the synthesis of  $\text{HfV}_2\text{O}_7$  from nanoparticle precursors. In the first step, tetragonal  $\text{HfO}_2$  nanoparticles ( $3.3 \pm 0.7$  nm; Figure 2A) prepared using hydrothermal methods have been mixed with  $\text{VO}_2$  nanorods ( $374 \pm 73$  nm in length; Figure 2D) using ball-milling. The STEM-EDS mapping

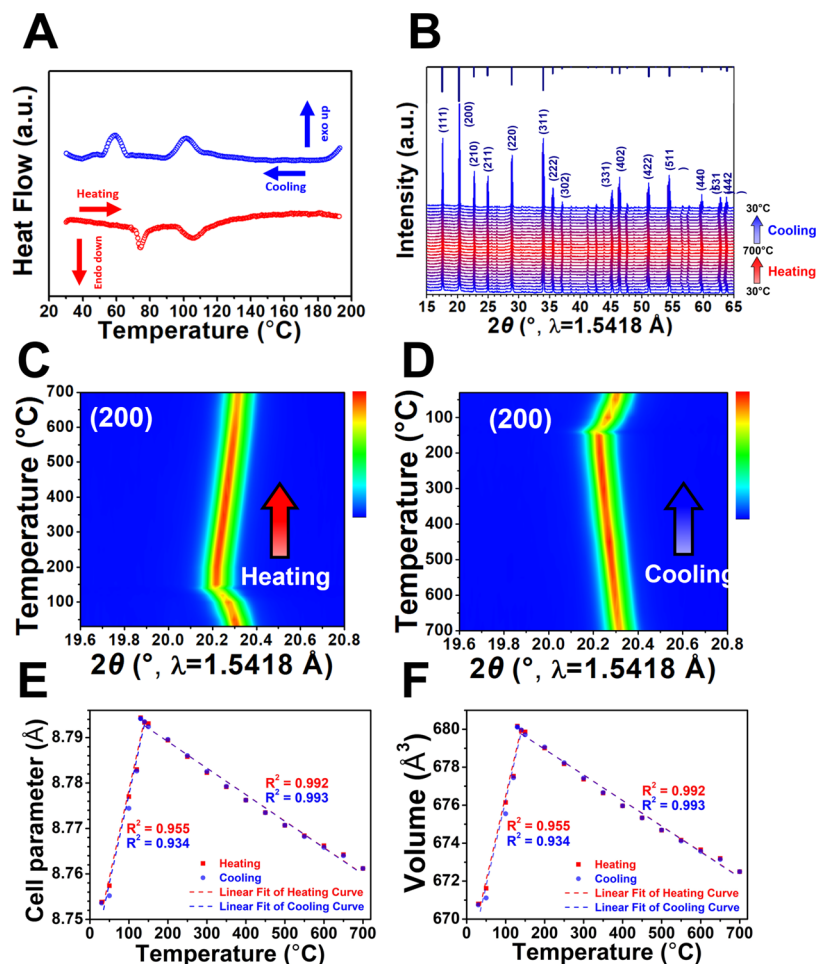


**Figure 2.** TEM images of (A) tetragonal HfO<sub>2</sub> nanoparticles, (B) monoclinic HfO<sub>2</sub> nanoparticles, (C) bulk monoclinic HfO<sub>2</sub>, (D) VO<sub>2</sub> nanorods, and (E, F) cubic HfV<sub>2</sub>O<sub>7</sub> nanoparticles. (G) SEM image of cubic HfV<sub>2</sub>O<sub>7</sub> nanoparticles. (H) Lattice-resolved HRTEM image of a cubic HfV<sub>2</sub>O<sub>7</sub> nanoparticle. (I) Powder X-ray diffraction pattern collected for HfV<sub>2</sub>O<sub>7</sub> nanoparticles synthesized from tetragonal HfO<sub>2</sub> nanoparticles at 500 °C. The raw data is plotted in black; the Rietveld fit is shown as blue crosses; the background function is depicted as a red line, and the residual (observed – calculated) is depicted as a brown line. The refined HfV<sub>2</sub>O<sub>7</sub> structure viewed down (J) the *a* axis and (K) 45° between the *a* and *b* axes.

images in Figure 1B,C as well as overlays of EDS maps in Figure S1 suggest that VO<sub>2</sub> nanorods are homogeneously covered by HfO<sub>2</sub> nanoparticles after ball-milling. The XRD pattern of the ball-milled mixture (Figure 1D) shows that HfO<sub>2</sub> nanoparticles remain in the tetragonal phase, whereas the VO<sub>2</sub> nanorods preserve their M<sub>1</sub> structure. As such, the effect of ball milling is to obtain an intimately mixed precursor powder; no chemical reactions are initiated under these conditions. In the second step, the ball-milled mixture has been sintered at 600 °C in static air to obtain cubic HfV<sub>2</sub>O<sub>7</sub>. Phase-pure HfV<sub>2</sub>O<sub>7</sub> is obtained from stoichiometric mixtures within ca. 30 min. The XRD pattern in Figure 1D can be indexed to PDF: 30-0614 corresponding to cubic HfV<sub>2</sub>O<sub>7</sub> with no discernible HfO<sub>2</sub> or VO<sub>2</sub> impurities. Miller indices are delineated in the figure for the most intense reflections. The refined HfV<sub>2</sub>O<sub>7</sub> structure is shown in Figure 2I.

It is noteworthy that the nanometer-sized dimensions of the precursor materials are critical to achieving a phase-pure product at a relatively low annealing temperature. The high surface area of the nanocrystalline precursors increases the interfacial area for reactions, and the nanometer-sized dimensions ensure relatively short diffusion lengths.<sup>35</sup> Figure S2 shows powder X-ray diffraction patterns of HfV<sub>2</sub>O<sub>7</sub> synthesized from differently sized particles and polymorphs

of HfO<sub>2</sub>.<sup>36</sup> When sub-micron-sized monoclinic HfO<sub>2</sub> (120.2 ± 25.7 nm; Figure 2C) particles are used as precursors, annealing in static air at 600 °C results in a relatively low yield of HfV<sub>2</sub>O<sub>7</sub>, and instead unreacted HfO<sub>2</sub> and oxidized V<sub>2</sub>O<sub>5</sub> are observed. The conventional high-temperature synthesis of HfV<sub>2</sub>O<sub>7</sub> from bulk monoclinic HfO<sub>2</sub> and V<sub>2</sub>O<sub>5</sub> to obtain relatively high-purity HfV<sub>2</sub>O<sub>7</sub> products requires more complicated processes including 3× grinding and pelletizing, 72 h annealing time, and 700 °C annealing temperature (Figure S3).<sup>18</sup> In contrast, tetragonal HfO<sub>2</sub> nanoparticles (3.3 ± 0.7 nm; Figure 2A) as well as monoclinic HfO<sub>2</sub> nanoparticles (5.0 ± 0.8 nm; Figure 2B) yield phase-pure HfV<sub>2</sub>O<sub>7</sub> products upon reaction with VO<sub>2</sub> nanorods at 600 °C for only 30 min. Figure 2E–G shows the morphology of HfV<sub>2</sub>O<sub>7</sub> nanostructures obtained by the reaction of tetragonal HfO<sub>2</sub> nanoparticles with VO<sub>2</sub> nanorods. The HfV<sub>2</sub>O<sub>7</sub> platelets have lateral dimensions of 25.4 ± 4.4 nm. The lattice-resolved HRTEM image in Figure 2H attests to the single-crystalline nature of the particle and shows lattice separations of 4.96 ± 0.05 and 3.52 ± 0.06 Å, corresponding to the separation between (111) and (211) planes of cubic HfV<sub>2</sub>O<sub>7</sub>, respectively. Figure 2I shows a Rietveld refinement of the powder XRD pattern measured for HfV<sub>2</sub>O<sub>7</sub> nanostructures at 500 °C (the room temperature structure is described below). Refinement



**Figure 3.** (A) DSC curve obtained for synthesized  $\text{HfV}_2\text{O}_7$ , indicating the phase transformations at 74 and 105 °C. (B) Temperature-dependent X-ray diffraction patterns of  $\text{HfV}_2\text{O}_7$ . (C, D) Patterns were collected from 30 to 700 °C at 50 °C intervals. (C, D) Heat map showing modulation plot of the (200) reflection as a function of temperature during heating and cooling. To find out the exact start point of NTE behavior, the reflections at 120, 130, and 140 °C were added in the plots. (E) Cell parameter and (F) cell volume (derived from unit cell refinements of the variable-temperature diffraction data) plotted as a function of temperature with linear fitting and  $R^2$  values.

statistics, lattice parameters, and atom positions obtained from the Rietveld refinement are provided in Table S1. The pattern refines to cubic  $\text{HfV}_2\text{O}_7$  in the  $Pa\bar{3}$  space group with  $Z = 4$  and  $a = 8.77$  Å. Figure 2J,K shows two views of the crystal structure.

Figure 3A shows a DSC thermogram of  $\text{HfV}_2\text{O}_7$  upon heating from 30 to 150 °C. Two (reversible) endothermic anomalies are associated with structural phase transitions at 74 and 105 °C. The low-temperature anomaly results from the phase transition from a  $3 \times 3 \times 3$  superstructure to an intermediate phase. The high-temperature anomaly corresponds to the transition to the high-temperature phase, which undergoes NTE. Figure S4 shows a  $\text{HfV}_2\text{O}_7$  cubic superstructure with  $a = 26.25$  Å in the  $Pa\bar{3}$  space group refined from the X-ray diffraction pattern of  $\text{HfV}_2\text{O}_7$  collected at 30 °C. The structure is refined to a  $Pa\bar{3}$  structure with  $a = 8.75$  Å, with a series of much weaker reflections indexed to a  $3 \times 3 \times 3$  superstructure; the structure contains 6 unique Hf sites and 11 V sites. Figure S5 reveals that this  $3 \times 3 \times 3$  superlattice exists only below 105 °C, which then transitions to the high-temperature phase that exhibits NTE behavior.

To investigate the NTE behavior of  $\text{HfV}_2\text{O}_7$ , temperature-dependent powder XRD patterns were acquired in the temperature range between 30 and 700 °C, as shown in

Figure 3B–D. Consistent reflections are observed for the heating and cooling cycles, which demonstrates the high thermal stability of  $\text{HfV}_2\text{O}_7$ . In the range of 30–130 °C, the (200) reflection shifts from  $2\theta = 20.31$  to  $20.24^\circ$ , which corresponds to an increase of the interplanar separation. However, after undergoing the transformation to the high-temperature phase and with loss of the superlattice ordering, NTE behavior is clearly manifested from 130 to 700 °C with the reflections shifted from  $2\theta = 20.24$  to  $20.32^\circ$  (Figure 3C,D). The cell parameters of  $\text{HfV}_2\text{O}_7$  have been refined from these patterns. Figure 3E,F plots changes in the cell parameter and cell volume of  $\text{HfV}_2\text{O}_7$  as a function of temperature. The cell parameter decreases linearly from 8.794 to 8.761 Å with an increase in temperature from 130 to 700 °C. It is particularly notable that the NTE behavior remains linear across this entire range with  $R^2 = 0.992$  for the heating cycle and  $R^2 = 0.993$  for the cooling cycle, significantly surpassing the operational range for  $\text{ZrV}_2\text{O}_7$ , where a phase transition is manifested at ca. 600 °C.<sup>19</sup> The calculated linear thermal expansion coefficient of  $\text{HfV}_2\text{O}_7$  is  $-6.7 \times 10^{-6} \text{ }^\circ\text{C}^{-1}$ . The volume is decreased by 1.13% as the temperature increases from 130 to 700 °C. The overlapping cooling and heating curves demonstrate the reversibility of volume changes in  $\text{HfV}_2\text{O}_7$ .

Figure 4 shows successive Raman spectra of  $\text{HfV}_2\text{O}_7$  acquired as a function of temperature. Six bands centered at

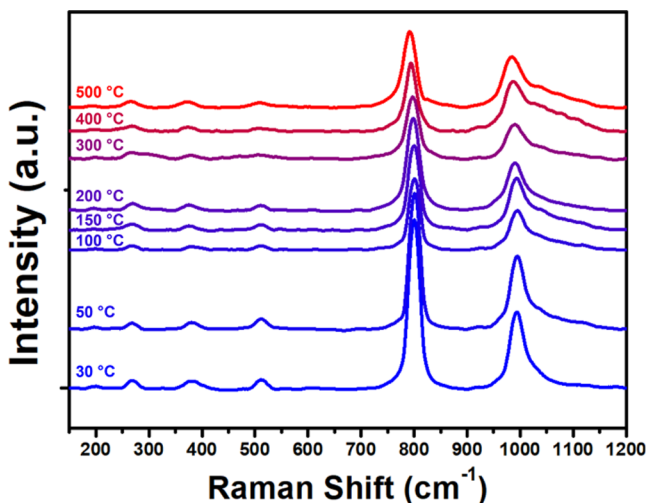


Figure 4. Raman spectroscopy of  $\text{HfV}_2\text{O}_7$  as a function of temperature.

201, 268, 381, 512, 801, and 993  $\text{cm}^{-1}$  are observed. The bands centered at 993 and 801  $\text{cm}^{-1}$  are assigned to symmetric and asymmetric stretching modes of  $\text{VO}_4$  tetrahedra, respectively.<sup>37–39</sup> The Raman band centered at 512  $\text{cm}^{-1}$  is ascribed to the asymmetric bending of  $\text{VO}_4$  tetrahedra in combination with  $\text{HfO}_6$  octahedral stretching; the bands at 381 and 268  $\text{cm}^{-1}$  are attributed to the symmetric bending of  $\text{VO}_4$  tetrahedra. The low-energy vibration at 201  $\text{cm}^{-1}$  is assigned to a lattice mode.<sup>37–39</sup> It is noteworthy that the characteristic Raman bands of  $\text{HfV}_2\text{O}_7$  at 993 and 801  $\text{cm}^{-1}$  are mostly unchanged upon heating from 30 to 150  $^{\circ}\text{C}$ , but are gradually shifted to lower frequencies with increasing temperature beyond 150  $^{\circ}\text{C}$ . Specifically, the prominent  $\text{VO}_4$  symmetric and asymmetric stretching modes are red-shifted from 993 and 801  $\text{cm}^{-1}$  at 150  $^{\circ}\text{C}$  to 984 and 792  $\text{cm}^{-1}$  at 500  $^{\circ}\text{C}$ , respectively. These shifts within the NTE regime denote an elongation of V–O bond lengths, which have a pivotal role in enabling transverse vibrations to decrease the overall cell volume.

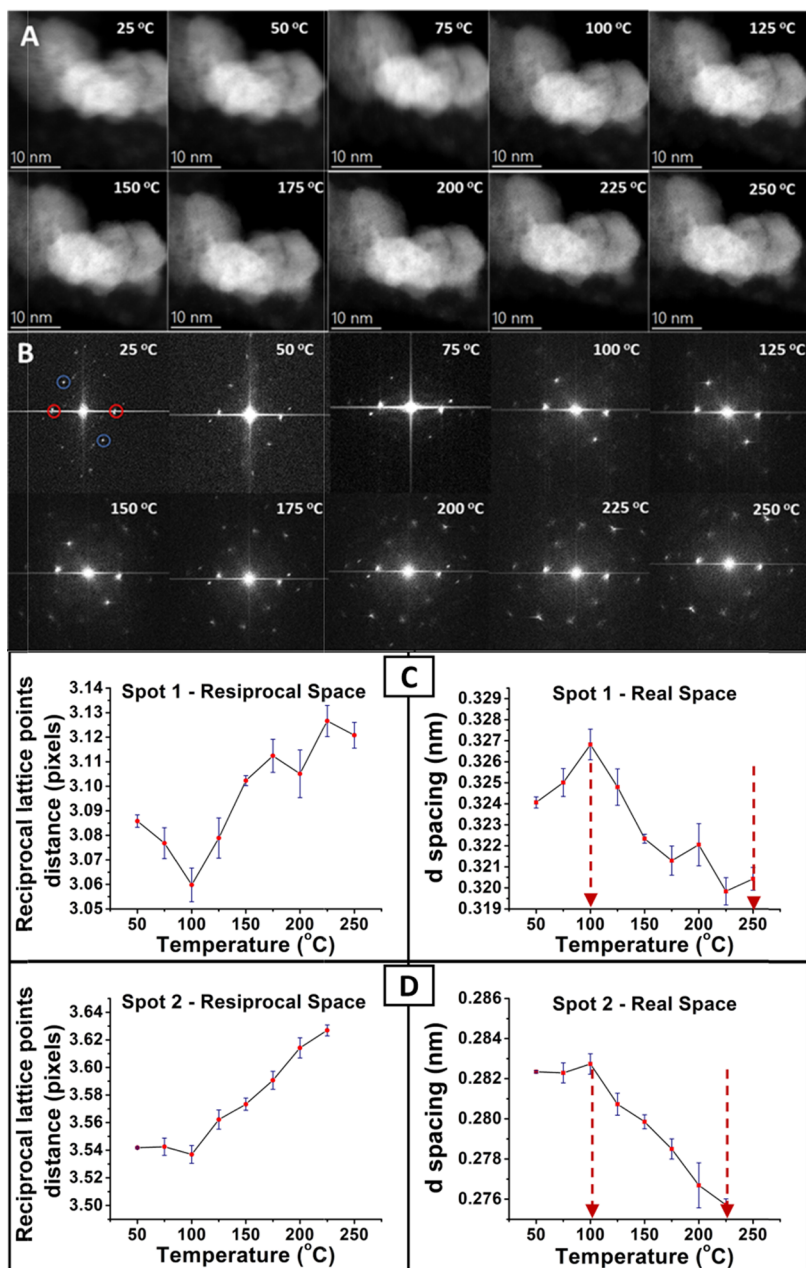
An in situ heating study performed using TEM illustrating the NTE behavior of  $\text{HfV}_2\text{O}_7$  is shown in Figure 5. Previous work on a similar NTE material,  $\text{ZrW}_2\text{O}_8$ , indicates that upon exposure to the atmosphere, the sample absorbs moisture, forming the hydrated  $\text{ZrW}_2\text{O}_7(\text{OH})_2 \cdot 2\text{H}_2\text{O}$  phase that does not show NTE behavior.<sup>40</sup> To eliminate adsorbed water, the sample was heated (from 25  $^{\circ}\text{C}$ ) and held at 650  $^{\circ}\text{C}$  for 5 h (in the microscope) and then cooled to 25  $^{\circ}\text{C}$ , prior to the in situ heating TEM experiments. Figure 5A,B shows the high-angle annular dark-field micrographs and their respective fast Fourier transforms (FFTs) obtained at 25  $^{\circ}\text{C}$  intervals in the temperature range of 25–250  $^{\circ}\text{C}$ . In each of these individual FFTs, two sets of spots corresponding to two sets of crystal planes of  $\text{HfV}_2\text{O}_7$  were identified. The images in Figure 5C,D were generated by measuring distances of the red and blue spots, respectively, from the straight through beam spot. The reciprocal space distances of these spots were measured, and their real-space crystal plane  $d$ -spacings were computed. The temperature-dependent plots of both reciprocal space and real space distances are shown in Figure 5C,D, which indicate an

increase of  $d$ -spacing distances up to  $\sim 100$   $^{\circ}\text{C}$  and a decrease with further increase of temperature beyond  $\sim 100$   $^{\circ}\text{C}$ , which is consistent with the in situ XRD data obtained in the same temperature range.<sup>28,41</sup>

Considering the strong and isotropic NTE behavior manifested in  $\text{HfV}_2\text{O}_7$  nanoparticles, we have examined its potential as a thermal expansion compensator. PBI is a hard-glassy polymer possessing outstanding thermal and chemical stability with an upper working temperature of ca. 400  $^{\circ}\text{C}$ ; it is widely used as a high-temperature protective coating for metal substrates as well as in proton exchange membranes of high-temperature fuel cells.<sup>42,43</sup> Given its high glass-transition temperature, it is the polymer of choice for structural applications at high temperatures. However, PBI has a thermal expansion coefficient in excess of  $34 \times 10^{-6}$   $^{\circ}\text{C}^{-1}$  in the temperature range between 150 and 300  $^{\circ}\text{C}$ ,<sup>44–46</sup> which can result in considerable stress accumulation at the interfaces of coated substrates, resulting inevitably in delamination upon prolonged thermal cycling.<sup>47</sup> In this study,  $\text{HfV}_2\text{O}_7$  nanoparticles have been incorporated within a PBI film to reduce the large compressive stresses generated by thermal expansion.

Figures 6 and S6 show the evolution of thermal stresses that develop in a composite  $\text{HfV}_2\text{O}_7$ /PBI thin film on Si during heating with various loadings of  $\text{HfV}_2\text{O}_7$  nanoparticles. The stress response of PBI at temperatures below 130  $^{\circ}\text{C}$  is dominated by its hygroscopicity (Figure S6). PBI has a high affinity for moisture owing to the hydrogen bonds formed between water and nitrogen and N–H groups in PBI frameworks and can absorb as much as 15 wt % of water at equilibrium.<sup>48–50</sup> As the temperature increases during the heating process, the evaporation of water results in the shrinkage of the PBI film, which gives rise to tensile stress in the film when constrained by the underlying substrate. At temperatures above 130  $^{\circ}\text{C}$ , the absorbed water has completely evaporated, and the observed stress behavior stems solely from the intrinsic thermal expansion behavior of PBI. Figure 6 reveals that the pristine PBI film without embedded thermal compensation fillers develops substantial compressive stress above 150  $^{\circ}\text{C}$ , ranging up to 30.7 MPa at 300  $^{\circ}\text{C}$ . The observed compressive stress is substantially mitigated with the incorporation of  $\text{HfV}_2\text{O}_7$ . The compression reduction reaches 67.3% for 26.6 vol %  $\text{HfV}_2\text{O}_7$  incorporation with respect to the pristine PBI thin film. Still higher loadings of  $\text{HfV}_2\text{O}_7$  nanoparticles result in a diminution of the PBI adhesion strength. The inset to Figure 6 shows three thermal stress cycles of an 8.4 vol %  $\text{HfV}_2\text{O}_7$ /PBI composite thin film from 150 to 300  $^{\circ}\text{C}$ , revealing minimal stress accumulation upon thermal cycling. Overall, the results in Figure 6 attest to the viability of the prepared  $\text{HfV}_2\text{O}_7$  as effective thermal expansion compensators in nanocomposite thin films.

Figure S7 compares the dispersion of micron-sized  $\text{HfV}_2\text{O}_7$ , which was synthesized by conventional solid-state synthesis,<sup>18</sup> and  $\text{HfV}_2\text{O}_7$  nanocrystals in the PBI matrix. The EDS elemental maps clearly demonstrate the much more homogeneous distribution of  $\text{HfV}_2\text{O}_7$  nanocrystals compared to micron-sized particles in PBI. Distinct phase segregation is evidenced for micron-sized particles. Notably, multibeam optical stress sensor measurements probe the ensemble response across the entire film and do not probe localized stresses, e.g., those that may develop near a particle/matrix interface resulting from phase segregation.



**Figure 5.** In situ TEM analysis of  $\text{HfV}_2\text{O}_7$  illustrating the NTE behavior. (A, B) Individual HAADF micrographs collected every 25 °C in the temperature range of 25–250 °C and their respective FFTs. (C, D) Plots showing the temperature dependence of lattice spacing distances and their reciprocal, corresponding to spots 1 (red FFT spots) and 2 (blue FFT spots). NTE behavior is clearly evidenced between the regimes bounded by red dashed arrows.

To further elucidate the origin of the effects of incorporating  $\text{HfV}_2\text{O}_7$  in mitigating stresses in the film, we develop a simple model. First, for the pure PBI film (without  $\text{HfV}_2\text{O}_7$ )<sup>51</sup>

$$\sigma_{\text{PBI}} = E_{\text{PBI}}(\alpha_{\text{substrate}} - \alpha_{\text{PBI}})\Delta T \quad (3)$$

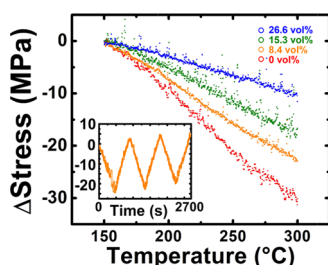
where  $\sigma_{\text{PBI}}$  is the stress in the pure PBI film;  $E_{\text{PBI}} = 6$  GPa is the elastic modulus of the PBI film;<sup>46</sup>  $\alpha_{\text{PBI}} = 34 \times 10^{-6} \text{ }^\circ\text{C}^{-1}$  is the coefficient of thermal expansion of the pure PBI film;<sup>44,45</sup>  $\alpha_{\text{substrate}}$  is the coefficient of thermal expansion of the Si substrate, i.e.,  $\alpha_{\text{substrate}} \sim 3.6 \times 10^{-6} \text{ }^\circ\text{C}^{-1}$  from 150 to 300 °C;<sup>52</sup> and  $\Delta T$  is the temperature change, i.e.,  $\Delta T = 150$  °C over the range associated with Figure 6. Substituting these values into eq 3 gives  $\sigma_{\text{PBI}} = -27.4$  MPa, in which the negative sign indicates compression. This predicted value is quite

similar to the measured value of  $-30.7$  MPa for 0 vol % shown in Figure 6.

Next, to analyze the effects of incorporating  $\text{HfV}_2\text{O}_7$  into the film, we implement commonly used models for composites<sup>40,53,54</sup>

$$\alpha_{\text{composite}} = \frac{f_r E_r \alpha_r + f_m E_m \alpha_m}{E_r f_r + E_m f_m} \quad (4)$$

$$E_{\text{upper\_composite}} = E_r f_r + E_m f_m, \\ E_{\text{lower\_composite}} = \frac{E_r E_m}{E_m f_r + E_r f_m} \quad (5)$$



**Figure 6.** Evolution of thermal stresses developed in HfV<sub>2</sub>O<sub>7</sub>/PBI films on a Si substrate between 150 and 300 °C. The measurements are normalized taking the stress at 150 °C to be the reference point (zero stress). The inset shows three thermal stress cycles measured for an 8.4 vol % HfV<sub>2</sub>O<sub>7</sub>/PBI composite from 150 to 300 °C at a heating and cooling rate of 20 °C/min.

where  $E_r = 78$  GPa and  $E_m = 6$  GPa are the elastic moduli of HfV<sub>2</sub>O<sub>7</sub> and PBI, respectively;<sup>40,46</sup>  $f_r$  and  $f_m$  indicate the volume fractions of HfV<sub>2</sub>O<sub>7</sub> and PBI, respectively (note that  $f_r + f_m = 1$ ); and  $\alpha_r = -6.7 \times 10^{-6}$  °C<sup>-1</sup> and  $\alpha_m = 34 \times 10^{-6}$  °C<sup>-1</sup> are the thermal expansion coefficients of HfV<sub>2</sub>O<sub>7</sub> and PBI, respectively.<sup>44,45</sup> From eq 4 and 5, for  $f_r = 0.266$ ,  $\alpha_{\text{composite}} = 34.4 \times 10^{-8}$  °C<sup>-1</sup>,  $E_{\text{upper\_composite}} = 25.1$  GPa, and  $E_{\text{lower\_composite}} = 7.95$  GPa.

The corresponding stress in the composite film (on the Si substrate) is<sup>51</sup>

$$\sigma_{\text{composite}} = E_{\text{composite}}(\alpha_{\text{substrate}} - \alpha_{\text{composite}})\Delta T \quad (6)$$

Through eq 6, the stress in the composite film equals 12.3 and 3.9 MPa by adopting upper and lower bounds on the composite modulus of eq 5 over the 150 °C temperature increase associated with Figure 6. Note that this analysis predicts small tensile stresses, which is different from the small compressive stresses observed at 26.6 vol % HfV<sub>2</sub>O<sub>7</sub> in Figure 6. As such, the analysis presented in eqs 4–6 slightly overestimates the effects of incorporating HfV<sub>2</sub>O<sub>7</sub> in alleviating the compressive stresses in the film. Indeed, eq 4 represents one of several existing models for the coefficient of thermal expansion of a composite; its strict validity depends on several details, e.g., shape, size, orientation, and connectivity of the reinforcement and details of bonding between the reinforcement and the matrix. Still, this simple analysis underscores the influence of the HfV<sub>2</sub>O<sub>7</sub>: by rapidly reducing the overall coefficient of thermal expansion, smaller compressive (more tensile) stresses are developed in the film upon the addition of HfV<sub>2</sub>O<sub>7</sub>. Likewise, in both the model and the measured results (Figure 6), it is evident that HfV<sub>2</sub>O<sub>7</sub> can quickly reduce the thermal expansion coefficient of the composite thin film, even at relatively low volume fractions of HfV<sub>2</sub>O<sub>7</sub>. The source of this relatively quick reduction is evident through eq 4 by noting that the elastic modulus of HfV<sub>2</sub>O<sub>7</sub> is 1 order of magnitude larger than PBI. Finally, we should note that by changing the volume fraction of HfV<sub>2</sub>O<sub>7</sub>, we can, in principle, tune the overall coefficients of thermal expansion of the film such that they are well matched to a range of substrates, thereby mitigating thermal stresses in various film/substrate systems.

## CONCLUSIONS

In summary, we have developed a facile synthesis of phase-pure HfV<sub>2</sub>O<sub>7</sub> nanoparticles starting from HfO<sub>2</sub> and VO<sub>2</sub> nanoparticles. Phase-pure products are obtained in ca. 30

min after annealing at a temperature of 600 °C. The synthesized HfV<sub>2</sub>O<sub>7</sub> nanoparticles exhibit isotropic and entirely reversible NTE behavior from 130 to 700 °C with CTE =  $-6.7 \times 10^{-6}$  °C<sup>-1</sup>, as evidenced by temperature-variant powder X-ray diffraction, Raman spectroscopy, and transmission electron microscopy measurements. While Hf and Zr have similar atomic radii as a result of lanthanide contraction and their compounds show considerable homologies,<sup>55</sup> their phonon dispersion is substantially different. As such, HfV<sub>2</sub>O<sub>7</sub> exhibits an extended linear CTE regime, whereas ZrV<sub>2</sub>O<sub>7</sub> shows a sharp diminution of the CTE coefficient above 600 °C as a result of a structural phase transition.<sup>19</sup> The HfV<sub>2</sub>O<sub>7</sub> nanoparticles have been embedded within a high-glass-transition-temperature thermoset as a thermal expansion compensator. Multibeam optical sensor measurements indicate as much as a 67.3% decrease of compressive stress upon embedding HfV<sub>2</sub>O<sub>7</sub> nanoparticles within the PBI film. Based on a composite model, we demonstrate that HfV<sub>2</sub>O<sub>7</sub> can rapidly reduce the thermal expansion coefficient of polymer nanocomposite films, even at low volume fractions, as a result of its substantially higher elastic modulus compared to the continuous polymer matrix. Overall, the facile synthesis strategy, manifestation of isotropic NTE across a broad temperature range, and the alleviation of compressive stress in a functional polymer nanocomposite coating at low loadings suggests a broad range of applications in high-temperature composites and nanocomposite coatings.

## ASSOCIATED CONTENT

### Supporting Information

The Supporting Information is available free of charge at <https://pubs.acs.org/doi/10.1021/acsami.1c10867>.

SEM-EDS mapping analysis on HfO<sub>2</sub>/VO<sub>2</sub> ball-milled mixtures; XRD pattern of HfV<sub>2</sub>O<sub>7</sub> synthesized from different HfO<sub>2</sub>; X-ray diffraction patterns of HfV<sub>2</sub>O<sub>7</sub> synthesized from conventional solid-state method; Rietveld refinement of the HfV<sub>2</sub>O<sub>7</sub> structure; and XRD patterns of HfV<sub>2</sub>O<sub>7</sub> collected at 30, 50, 100, 150, and 200 °C (PDF)

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### Author Contributions

G.-W.L. contributed to conceptualization, methodology, software, validation, formal analysis, investigation, writing—original draft, and visualization. Y.Z. performed formal analysis, investigation, and writing—original draft. M.P.T. conducted formal analysis, investigation, and writing—original draft. A.U. performed formal analysis. M.P. carried out supervision and writing—review and editing. B.S.G. performed supervision and writing—review and editing. S.B. conducted supervision, project administration, and writing—review and editing.

### Notes

The authors declare no competing financial interest.

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